

**JOSAI  
MATHEMATICAL  
MONOGRAPHS**

**1**

**1999**



# **CONVEX ANALYSIS AND CHAOS**

The Third Symposium  
on Nonlinear Analysis  
July 23 – 25, 1998  
JOSAI UNIVERSITY

Edited by  
Kiyoko NISHIZAWA



JOSAI UNIVERSITY  
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**JMM 1. CONVEX ANALYSIS AND CHAOS**

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**JOSAI MATHEMATICAL MONOGRAPHS**  
**JMM 1.(1999) CONVEX ANALYSIS AND CHAOS,**

Published by Graduate School of Science,  
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Printed by GAITAME PRINTING CO., LTD.

29 – 6, Akasaka 2 – chome, Taito – ku, Tokyo  
111 – 0032 JAPAN  
tel. 03 – 3844 – 3855

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